

Dottorato di Ricerca in Ingegneria e Architettura XXXV° ciclo

Coordinator: Sandro Longo

## RESEARCH ACTIVITY

Phase-Field approach for brittle fracture



**UNIVERSITÀ  
DI PARMA**

PhD student: Lorenzo Mingazzi

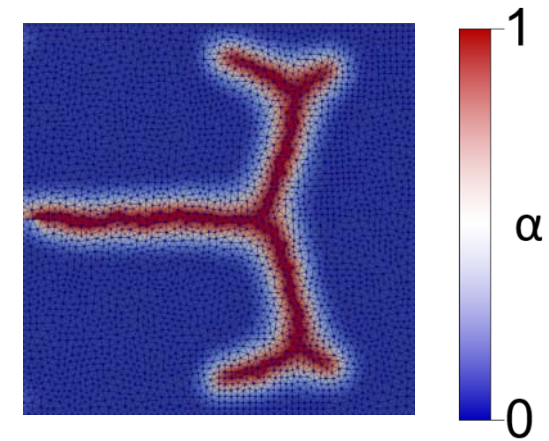
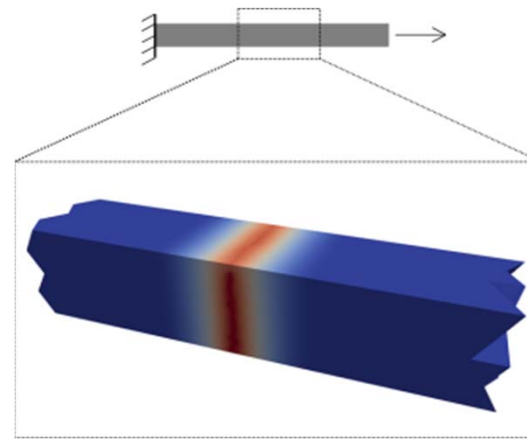
Tutor: Francesco Freddi

A. A. 2020/2021

04/02/2021

# PHASE-FIELD

- Variational approach based on the Griffith's fracture theory for brittle material;
- Damage is represented by a smooth scalar field where cracks are described as a transition zone between broken and unbroken material;
- Cracks nucleation and propagation are described via the minimization of a two field (displacement and damage) energy functional;



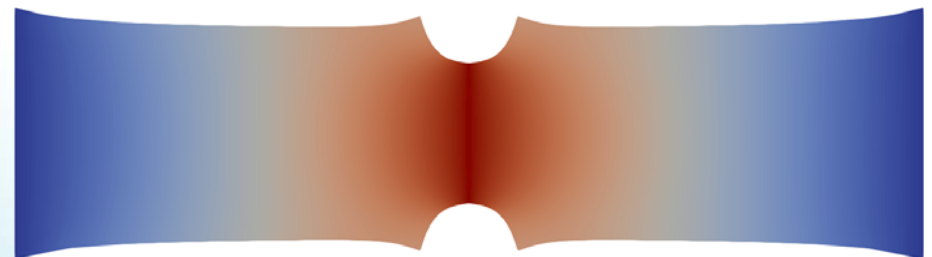
$$\Pi_l(\mathbf{u}, \alpha) = \underbrace{\int_{\Omega} ((1 - \alpha)^2 + k_l) \left( \frac{1}{2} \mathbf{C} \mathbf{E}(\mathbf{u}) \cdot \mathbf{E}(\mathbf{u}) \right) dx}_{\text{Strain Energy}} + \underbrace{\frac{\gamma}{2} \int_{\Omega} (l \|\nabla \alpha\|^2 + \frac{\alpha}{l}) dx}_{\text{Fracture Energy}}$$

Current topics of research:

## RC COVER CRACKING



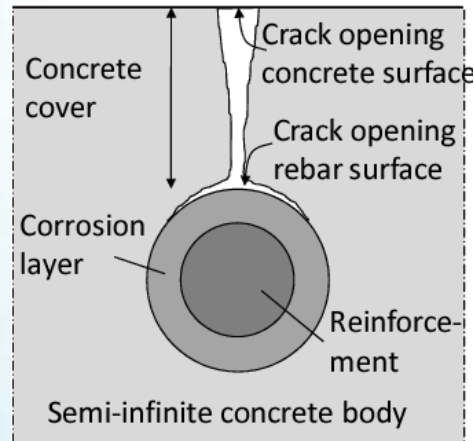
## FRACTURE IN HYPERELASTIC MATERIALS



## RC COVER CRACKING

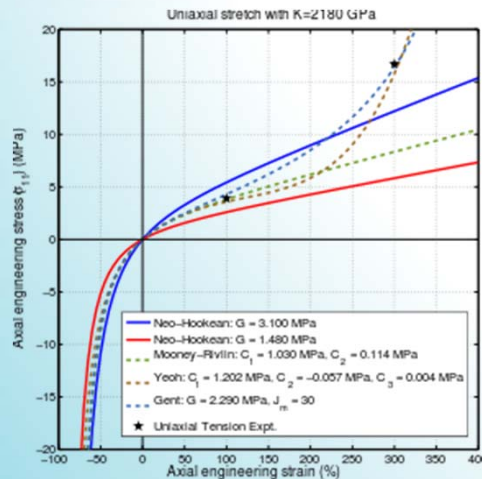
- Simulation of the corrosion induced cover cracking phenomenon via a numerical model which can describe:

- 1 - CO<sub>2</sub> diffusion within concrete
- 2 - Swelling of the steel rebar
- 3 - Cover cracking via the phase-field method



## FRACTURE IN HYPERELASTIC MATERIALS

- Usage of the different strain energy function to reproduce the mechanical behavior of different biological tissues (Neo-Hookean, Mooney-Rivlin, etc);
- Extension of the phase-field model to describe fracture in hyperelastic materials;



## PUBLICATIONS

1. R. Alessi, F. Freddi, L. Mingazzi, "Phase-field numerical strategies for deviatoric driven fractures", *Comput. Methods Appl. Mech. Engrg.* 2020, vol. 359, DOI: <https://doi.org/10.1016/j.cma.2019.112651>
2. Freddi F., Mingazzi L., "Phase-field simulations of laminated glass beams", *Materials*, 2020, vol. 13, DOI: <https://doi.org/10.3390/ma13143218>

## TOPIC of the THESIS

"Phase-field approach for fracture problems in hyperelastic materials"